

31.3. The current in the wire arises due to displacement of current which is given by -

$$I_D = \epsilon_0 A \frac{dE}{dt}$$

$$\frac{dE}{dt} = \frac{I_D}{\epsilon_0 A} = \frac{2.8 \text{ A}}{(8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2)(0.016 \text{ m}^2)^2} = 1.2 \times 10^{15} \frac{\text{V}}{\text{m s}}$$

meter second  
not millisecond

31.9. The electric and magnetic field are related by -

$$\frac{E_0}{B_0} = c \quad \therefore E_0 = B_0 c = (12.5 \times 10^{-9} \text{ T}) (3 \times 10^8 \text{ m/s}) = 3.75 \text{ V/m}$$

31.11. a) For the term with cos function,  $Kz + \omega t = K(z + ct)$

This shows that the wave is travelling along negative z direction with speed c.

b) The direction of wave propagation is given by  $\vec{E} \times \vec{B}$ . Since  $\vec{E}$  is along z axis, for  $\vec{E} \times \vec{B}$  to be along negative z axis,  $\vec{B}$  must be along negative y axis.  $B_0 = E_0/c$  (relating magnitude of  $\vec{B}$  with  $\vec{E}$ )

$$\therefore \vec{B} = - \frac{E_0}{c} \cos(Kz + \omega t) \hat{j}$$

$$31.14. a) c = \lambda f \quad \lambda f = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{2.575 \times 10^9 \text{ Hz}} = 1.165 \times 10^{-2} \text{ m}$$

$$b) f = \frac{c}{\lambda} = \frac{3 \times 10^8 \text{ m/s}}{0.12 \times 10^{-19} \text{ m}} = 2.5 \times 10^{18} \text{ Hz}$$

31.15.  $d = vt$ , d - distance, v - speed of wave, t - time taken

$$t = \frac{d}{v} = \frac{(1.5 \times 10^{11} \text{ m})}{3 \times 10^8 \text{ m/s}} = 5 \times 10^2 \text{ s} = 8.33 \text{ min}$$

31.20. a) A wave eq. can be written as  $E = E_0 \sin(Kz - \omega t)$

$$\lambda = \frac{2\pi}{K} = \frac{2\pi}{0.077 \text{ m}^{-1}} = 81.60 \text{ m}$$

$$f = \frac{\omega}{2\pi} = \frac{2.3 \times 10^7 \text{ rad/s}}{2\pi} = 3.661 \times 10^6 \text{ Hz}$$

b) The magnitude of the magnetic field would be  $B_0 = \frac{E_0}{c}$

The wave travels along <sup>positive</sup> z axis. Since  $\vec{E}$  is along positive x axis,  $\vec{B}$  must be along positive y axis to have  $\vec{E} \times \vec{B}$  along z axis.

$$B_0 = \frac{E_0}{c} = \frac{225 \text{ V/m}}{3 \times 10^8 \text{ m/s}} = 7.5 \times 10^{-7} \text{ T}$$

$$\vec{B} = (7.5 \times 10^{-7} \text{ T}) \sin((0.077 \text{ m}^{-1})z - (2.3 \times 10^7 \text{ rad/s})t) \hat{j}$$

31.25. The intensity of a wave is the power emitted per unit area.

$$\bar{S} = \frac{P}{A}$$

A denotes area of a sphere as energy is emitted in all directions

$$= \frac{1500 \text{ W}}{4\pi (0.5 \text{ m})^2} = 4.775 \text{ W/m}^2$$

$$\bar{S} = C \epsilon_0 E_{\text{rms}}^2$$

$$E_{\text{rms}} = \sqrt{\frac{\bar{S}}{C \epsilon_0}} = \sqrt{\frac{4.775 \text{ W/m}^2}{(3 \times 10^8 \text{ m/s})(8.85 \times 10^{-12} \text{ C}^2/\text{N m}^2)}} = 42 \text{ V/m}$$

31.28. Using above relations,

$$S = \frac{P}{A} = C \epsilon_0 E_{\text{rms}}^2$$

$$E_{\text{rms}} = \sqrt{\frac{P}{A \epsilon_0 C}} = \sqrt{\frac{0.0158 \text{ W}}{\pi (1 \times 10^{-3} \text{ m})^2 (3 \times 10^8 \text{ m/s}) (8.85 \times 10^{-12} \text{ C}^2/\text{N m}^2)}} = 1376.3 \text{ V/m}$$

$$B_{\text{rms}} = \frac{E_{\text{rms}}}{C} = \frac{1376.3 \text{ V/m}}{3 \times 10^8 \text{ m/s}} = 4.59 \times 10^{-6} \text{ T}$$

31.31. Since a solar panel can convert 10% of the sun's energy, intensity being put to use is  $\frac{10}{100} \times 1000 \text{ W/m}^2 = 100 \text{ W/m}^2$

a)  $A = \frac{P}{I} = \frac{50 \times 10^{-3} \text{ W}}{100 \text{ W/m}^2} = 5 \times 10^{-4} \text{ m}^2 = 5 \text{ cm}^2$

A calculator can be estimated to dimensions like 17 cm  $\times$  8 cm. So its given its area, <sup>the solar panel</sup> can be mounted on it.

b)  $A = \frac{P}{I} = \frac{1500 \text{ W}}{100 \text{ W/m}^2} = 15 \text{ m}^2$

A 1 roof top of a house would be about  $10 \text{ m}^2$ . Hence a solar panel on it can supply enough energy for a hair dryer.

c)  $A = \frac{P}{I} = \frac{20 \text{ hp} (746 \text{ W/hp})}{100 \text{ W/m}^2} = 149 \text{ m}^2$

A car's roof top cannot be so big that it can support such a big solar panel. Hence it is not possible.

31.35. The radiation pressure of the laser exerts a force on the cylinder and makes it accelerate. The rate of energy supply is  $\frac{dU}{dt} = 1 \text{ W} = P$

$$\bar{S} = \frac{\text{Power}}{A}$$

The radiation pressure is given as -

$\hat{P} = \frac{\bar{S}}{c}$  and the force exerted on the object due to this pressure is -

$$F = P A = \frac{\bar{S}}{c} A = \frac{1}{c} \frac{dU}{dt} = m a, \quad a \text{ denotes acceleration.}$$

$$m = \rho_{H_2O} \pi r^2 (r)$$

$$\therefore a = \frac{\frac{dU}{dt}}{c \rho_{H_2O} \pi r^3} = \frac{1 \text{ W}}{(3 \times 10^8 \text{ m/s}) (1000 \text{ kg/m}^3) \pi (5 \times 10^{-7} \text{ m})^3} \\ = 8 \times 10^6 \text{ m/s}^2$$

31.38. a) For FM radio,

$$\lambda_{\min.} = \frac{c}{f_{\max.}} = \frac{3 \times 10^8 \text{ m/s}}{1.08 \times 10^8 \text{ Hz}} = 2.78 \text{ m}$$

$$\lambda_{\max.} = \frac{c}{f_{\min.}} = \frac{3 \times 10^8 \text{ m/s}}{8.8 \times 10^7 \text{ Hz}} = 3.41 \text{ m}$$

b) For AM waves,

$$\lambda_{\min.} = \frac{c}{f_{\max.}} = \frac{3 \times 10^8 \text{ m/s}}{1.7 \times 10^6 \text{ Hz}} = 180 \text{ m}$$

$$\lambda_{\max.} = \frac{c}{f_{\min.}} = \frac{3 \times 10^8 \text{ m/s}}{5.35 \times 10^5 \text{ Hz}} = 561 \text{ m}$$

$$31.39. \lambda = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{1.9 \times 10^9 \text{ Hz}} = 0.16 \text{ m}$$

$$31.42. S = \frac{P}{A} = c \epsilon_0 E_{rms}^2 \quad \text{The radius turns out to be } \frac{1500 \text{ m}}{2} = 750 \text{ m}$$

$$E_{rms} = \sqrt{\frac{P}{A c \epsilon_0}} \\ = \sqrt{\frac{1.2 \times 10^4 \text{ W}}{\pi (750 \text{ m})^2 (3 \times 10^8 \text{ m/s}) (8.85 \times 10^{-12} \text{ C}^2/\text{N m}^2)}} = 1.6 \text{ V/m}$$

$$31.54. \bar{S} = \frac{1}{2} \epsilon_0 c E_0^2 \quad (\text{average intensity})$$

$$= \frac{P}{A} = \frac{P}{4\pi r^2}$$

The wave emits energy in all directions, the house appears to be a point on this energy sphere spread around.

$$\therefore r = \sqrt{\frac{2P}{4\pi \epsilon_0 c E_0^2}} = \sqrt{\frac{25000 \text{ W}}{2\pi (8.85 \times 10^{-12} \text{ C}^2/\text{N m}^2) (3 \times 10^8 \text{ m/s}) (0.02 \text{ V/m})^2}} \\ = 61,200 \text{ m} \approx 61 \text{ Km}$$

35.52. The initial beam is unpolarised. It gets polarized with half reduced intensity after passing through 1st polariser and then goes through the next one as a polarized one.

$$I_1 = \frac{1}{2} I_0$$

$$I_2 = I_1 \cos^2 \theta = \frac{I_0}{2} \cos^2 \theta \Rightarrow$$

$$\frac{I_2}{I_0} = \frac{\cos^2 \theta}{2} = \frac{\cos^2 65^\circ}{2} = 0.089$$

35.57. Like the previous problem,

$$I_1 = \frac{I_0}{2}, \quad I_2 = I_1 \cos^2 \theta = I_0 \frac{\cos^2 \theta}{2}$$

$$\cos^2 \theta = \frac{2 I_1}{I_0} \quad \cos \theta = \sqrt{\frac{2 I_2}{I_0}} \quad \theta = \cos^{-1} \left( \sqrt{\frac{2 I_2}{I_0}} \right)$$

a)  $\theta = \cos^{-1} \left( \sqrt{\frac{2}{3}} \right) = 35.3^\circ \quad \therefore \quad \frac{I_2}{I_0} = \frac{1}{3}$

b)  ~~$\cos \theta = \cos^{-1} \left( \sqrt{\frac{2}{10}} \right) = 63.4^\circ$~~   $\therefore \frac{I_2}{I_0} = \frac{1}{10}$

35.80.  $I_0$  be the initial intensity.

$$I_1 = I_0 \cos^2 \theta_1, \quad I_2 = I_1 \cos^2 \theta_2 = I_0 \cos^2 \theta_1 \cos^2 \theta_2 = 0.25 I_0$$

$$\cos^2 \theta_1 = \frac{0.25}{\cos^2 \theta_2} = \frac{0.25}{\cos^2 48^\circ}$$

$$\cos \theta_1 = \sqrt{\frac{0.25}{\cos 48^\circ}} \quad \therefore \theta_1 = \cos^{-1} \left( \frac{0.5}{\cos 48^\circ} \right) = 42^\circ$$

The initial angle with 1st polariser was  $42^\circ$ .